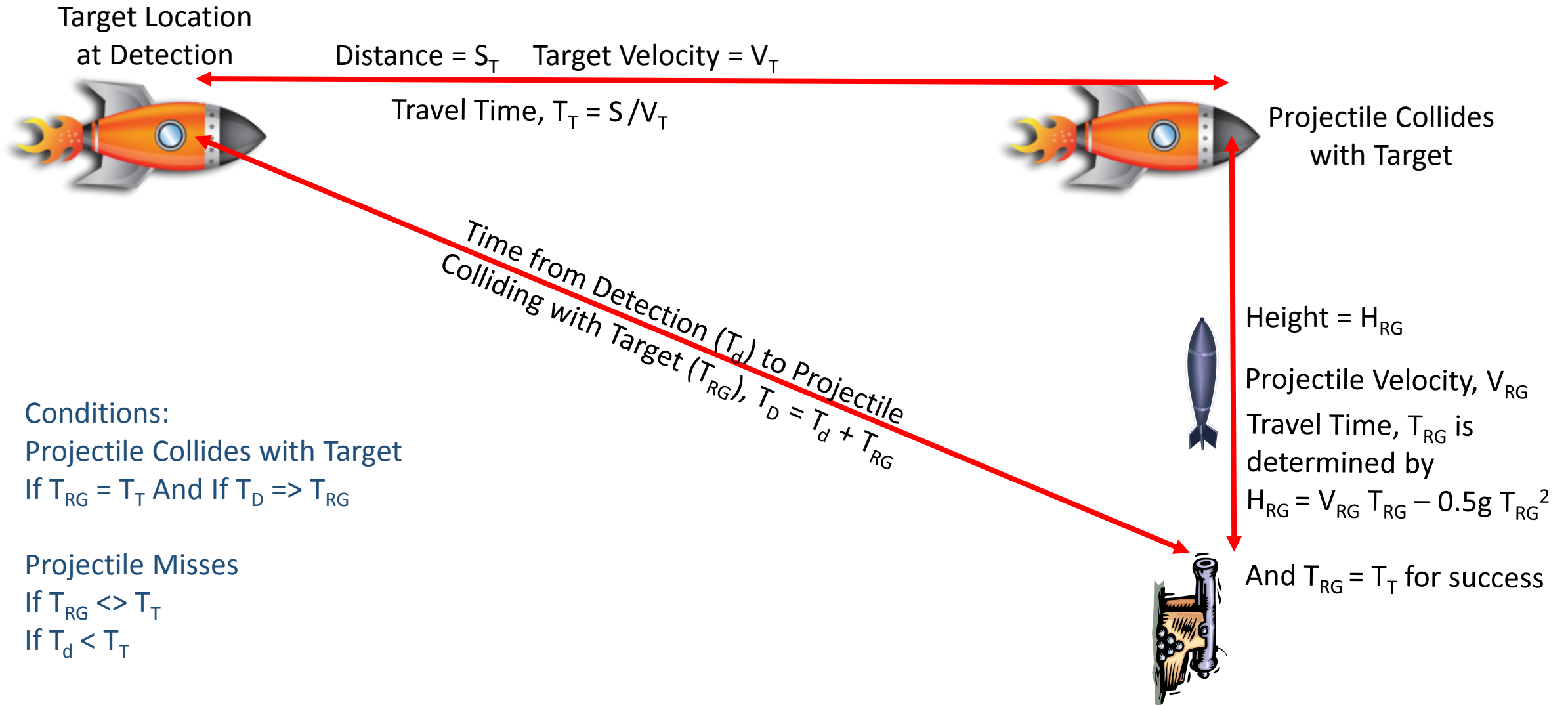


US Navy's Rail Gun Secret

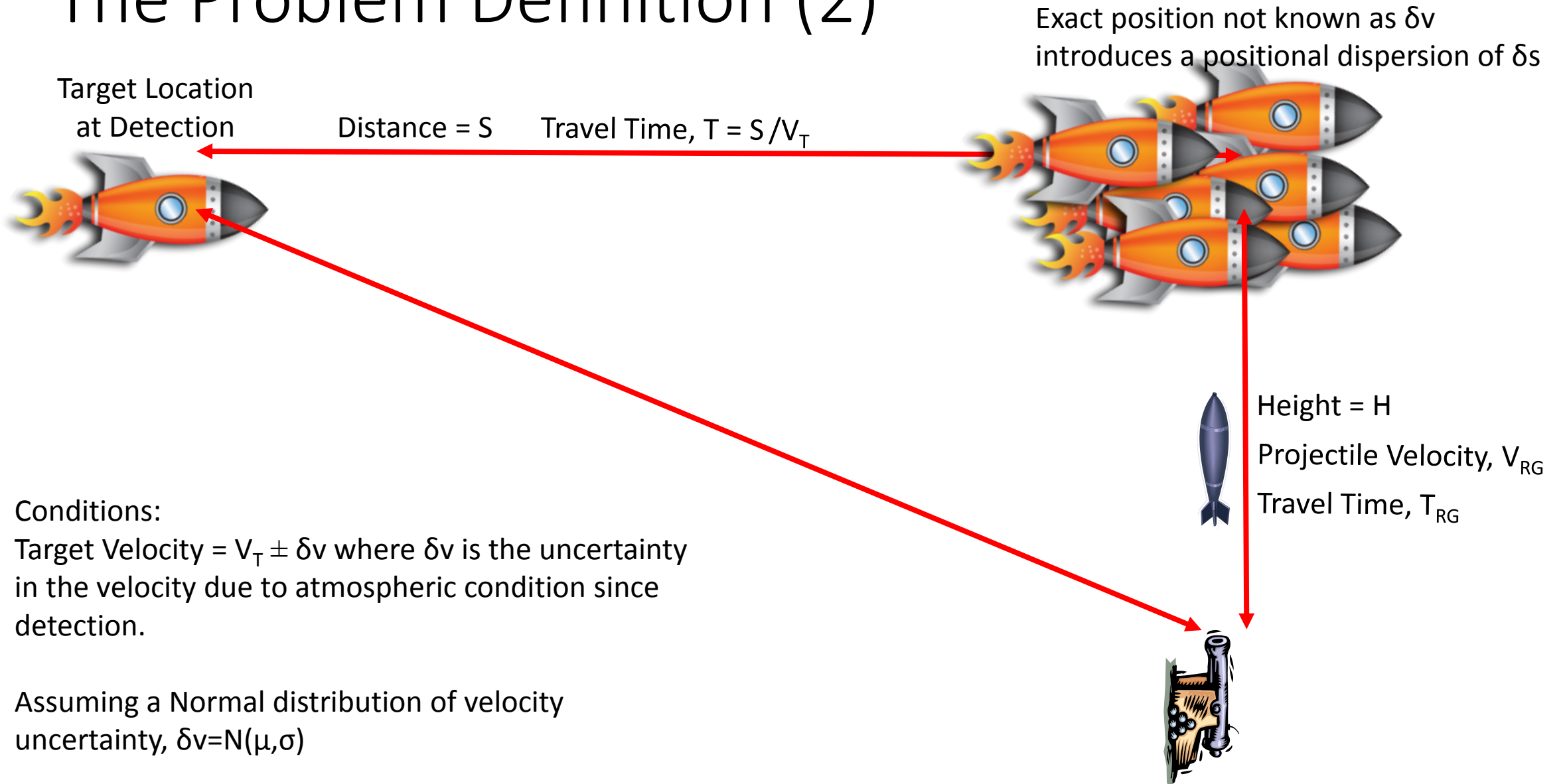
Benjamin T Solomon
Propulsion Physics, Inc
Xodus One Foundation

Problem Definition

The Problem Definition (1)



The Problem Definition (2)



The Problem Definition (3)

Problem:

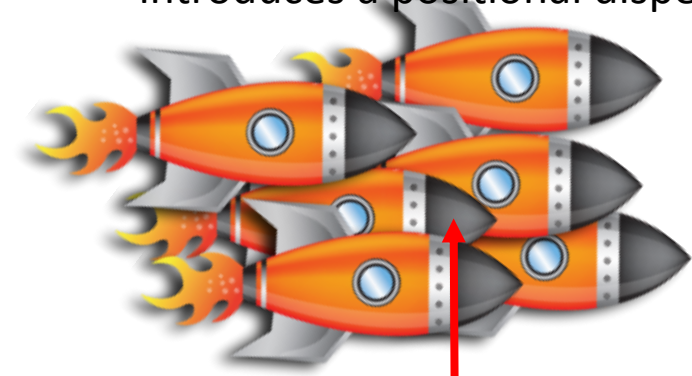
Given that atmospheric conditions introduce $\pm \delta v$
what is the most likely position of the Target when
the Projectile arrives at anticipated Target position?

Conditions:

Given that, $\delta v = N(\mu, \sigma)$

Variation in the true anticipated Target Location, $\delta s = 6T_T\sigma$

Exact position not known as δv
introduces a positional dispersion of δs



Height = H

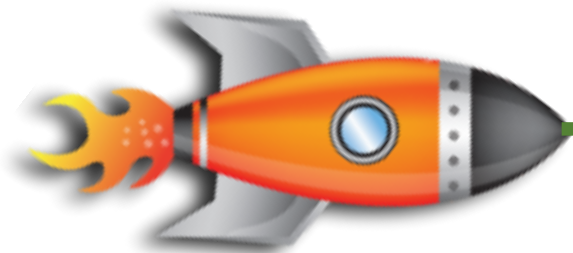
Projectile Velocity, V_{RG}

Travel Time, T_{RG}

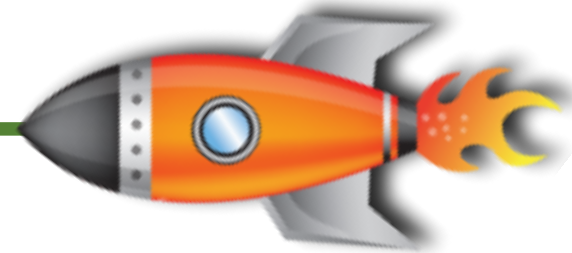


Solution Formulation

Target Velocity = $V_T \pm \delta v_1$
Such that, $\delta v_1 = N(\mu_1, \sigma_1)$



Target Velocity = $V_T \pm \delta v_2$
Such that, $\delta v_2 = N(\mu_2, \sigma_2)$



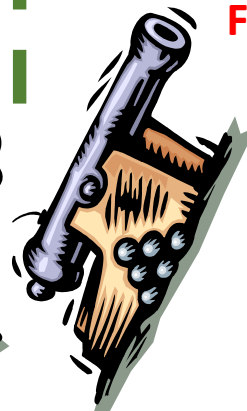
Distance = S_1
Travel Time, $T_1 = S_1/V_1$

Distance = S_2
Travel Time, $T_2 = S_2/V_2$

Slow Ship Gun

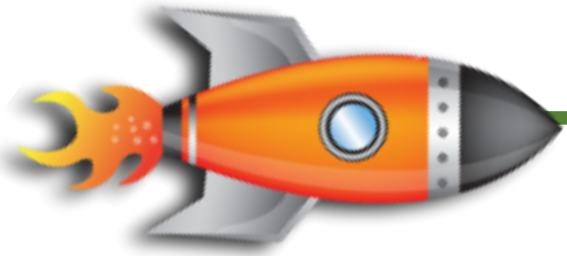


Fast Rail Gun



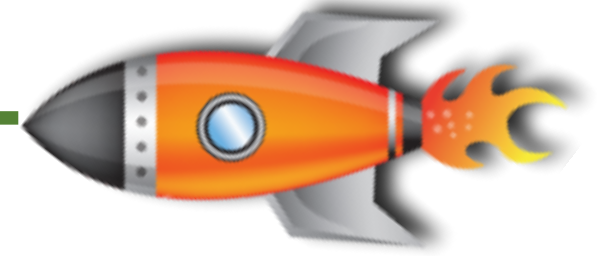
Since,
(1) $S_1 > S_2$ as $V_2 > V_1$
(2) Therefore, $T_1 > T_2$
(3) Since δv_1 & δv_2 are velocity errors,
 $\mu_1 = \mu_2 = 0$
(4) Therefore, $\sigma_1 > \sigma_2$ as target has
subject to greater variations in δv_1 due to
atmospheric conditions

Target Velocity = $V_T \pm \delta v_1$
Such that, $\delta v_1 = N(\mu_1, \sigma_1)$



Variation in the true
Target Location,
 $\delta s_1 = 6T_1\sigma_1$

Target Velocity = $V_T \pm \delta v_2$
Such that, $\delta v_2 = N(\mu_2, \sigma_2)$



Variation in the true
Target Location,
 $\delta s_2 = 6T_2\sigma_2$

Distance = S_1

Travel Time, $T_1 = S_1/V_1$

Distance = S_2

Travel Time, $T_2 = S_2/V_2$

Slow Ship Gun



Fast Rail Gun

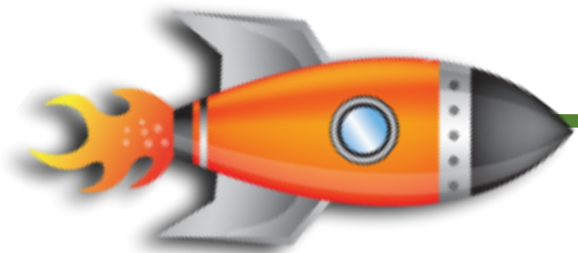


Since,

- (1) $T_1 > T_2$
- (2) $\sigma_1 > \sigma_2$
- (3) Therefore, $6T_1\sigma_1 \gg 6T_2\sigma_2$
- (4) Or $\delta s_1 \gg \delta s_2$
- (5) To consistently hit a projectile we require that the variation in the Target Location $\delta s < \text{Target Length}$

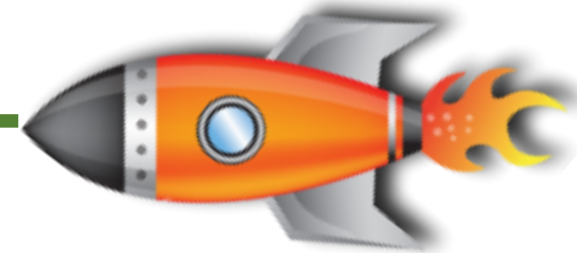
Summary: The faster the projectile muzzle velocity, V_R , the greater the accuracy & therefore the probability of hitting the moving target.

Target Velocity = $V_T \pm \delta v_1$
Such that, $\delta v_1 = N(\mu_1, \sigma_1)$



Variation in the true
Target Location,
 $\delta s_1 = 6T_1\sigma_1$

Target Velocity = $V_T \pm \delta v_2$
Such that, $\delta v_2 = N(\mu_2, \sigma_2)$



Variation in the true
Target Location,
 $\delta s_2 = 6T_2\sigma_2$

Distance = S_1

Travel Time, $T_1 = S_1/V_1$

Distance = S_2

Travel Time, $T_2 = S_2/V_2$

Slow Ship Gun



Fast Rail Gun



For simplicity, if we assume that the increase in the spread is a function of time, such that

- (1) $\sigma_1 = k.T_1$ and $\sigma_2 = k.T_2$ where k is some constant
- (2) Then $\delta s_1 = 6kT_1^2$ and $\delta s_2 = 6kT_2^2$
- (3) Or $\delta s_2 / \delta s_1 = (T_2/T_1)^2 = (S_2/S_1)^2 \cdot (V_1/V_2)^2$
- (4) Or upper bound of $\delta s_2 / \delta s_1 \approx (V_1/V_2)^2$

Conclusion: Hit accuracy is geometrically dependent upon projectile muzzle velocity, V_R .

Real Examples

Rail Gun versus Mark 80 Projectile

Comparisons	Muzzle Velocity (MPH)	
Rail Gun	5,600	
Mark 80 projectile with Mark 67 cartridge	831	
Mark 80 projectile with EX-175 cartridge	1,052	
Target Location Spread	Mark 80 projectile with Mark 67 cartridge	Mark 80 projectile with EX-175 cartridge
Rail Gun / Mark 80 ($\delta s_2 / \delta s_1 \approx (V_1/V_2)^2$)	2.2%	3.5%

X-51 : The Reverse is True

- With the Air Force's X-51 scram jet:
 - Capable of Mach 5 or 3,800 mph.
 - Cruising altitude of 70,000 ft.
 - Length of 25 ft.
- Target location spread is $\delta s_1 = 6T_1\sigma_1$. Using the above data for a rail gun projectile, gives an upper limit of $\sigma=0.3$ mph for $\delta s_1 = 25$ ft.
- The table below shows a projectile traveling at less than the velocity of the X-51 does not have the accuracy to shoot down the X-51.

Projectile Velocity (mph)	5,000	4,000	3,000	2,000	1,000
(Mach)	6.6	5.3	3.9	2.6	1.3
% of X-51 Velocity	132%	105%	79%	53%	26%
δs (ft)	19	24	31	43	70

We can thank the late
Prof. Eric Laithwaite
for the rail gun.

Important Lessons to Take Away

- Technology \neq Key Strategic Value
 - Key strategic value = Substantially improved accuracy
 - Deliverer of value = Substantially increased velocity
 - Mechanism to attain Delivery = The new technology of the Rail Gun
- Key strategic value is loosely coupled to the new technology
 - Therefore, potential for other types of technologies to replace rail gun
- High velocity is a substitute for missile guidance systems